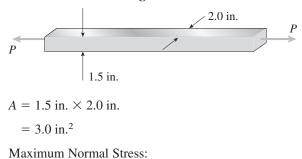
# **Stresses on Inclined Sections**

Problem 2.6-1 A steel bar of rectangular cross section  $(1.5 \text{ in.} \times 2.0 \text{ in.})$  carries a tensile load P (see figure). The allowable stresses in tension and shear are 15,000 psi and 7,000 psi, respectively.

Determine the maximum permissible load  $P_{\text{max}}$ .

### Solution 2.6-1 Rectangular bar in tension

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$$\sigma_x = \frac{P}{A}$$

Maximum shear stress:  $\tau_{\text{max}} = \frac{\sigma_x}{2} = \frac{P}{2A}$ 

$$\sigma_{\text{allow}} = 15,000 \text{ psi}$$
  $\tau_{\text{allow}} = 7,000 \text{ psi}$ 

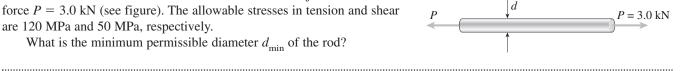
Because  $\tau_{\rm allow}$  is less than one-half of  $\sigma_{\rm allow},$  the shear stress governs.

1.5 in.

$$P_{\text{max}} = 2\tau_{\text{allow}} A = 2(7,000 \text{ psi}) (3.0 \text{ in.}^2)$$
  
= 42.000 lb

**Problem 2.6-2** A circular steel rod of diameter *d* is subjected to a tensile force P = 3.0 kN (see figure). The allowable stresses in tension and shear are 120 MPa and 50 MPa, respectively.

What is the minimum permissible diameter  $d_{\min}$  of the rod?

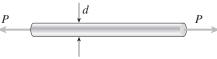


2.0 in.

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Р

Solution 2.6-2 Steel rod in tension



 $P = 3.0 \text{ kN} \quad A = \frac{\pi d^2}{4}$ 

Maximum normal stress:  $\sigma_x = \frac{P}{A}$ 

Maximum shear stress: 
$$\tau_{\text{max}} = \frac{\sigma_x}{2} = \frac{P}{2A}$$

$$( ) \xrightarrow{P}$$

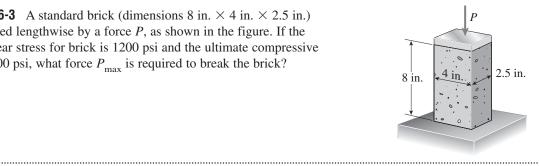
Because  $au_{\mathrm{allow}}$  is less than one-half of  $\sigma_{\mathrm{allow}}$ , the shear stress governs.

$$\tau_{\text{max}} = \frac{P}{2A} \quad \text{or} \quad 50 \text{ MPa} = \frac{3.0 \text{ kN}}{(2) \left(\frac{\pi d^2}{4}\right)}$$

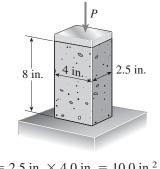
Solve for d:  $d_{\min} = 6.18 \text{ mm} \leftarrow --$ 

 $\sigma_{\rm allow} = 120 \; {\rm MPa}$  $\tau_{\rm allow} = 50 \; {\rm MPa}$ 

**Problem 2.6-3** A standard brick (dimensions 8 in.  $\times$  4 in.  $\times$  2.5 in.) is compressed lengthwise by a force P, as shown in the figure. If the ultimate shear stress for brick is 1200 psi and the ultimate compressive stress is 3600 psi, what force  $P_{\text{max}}$  is required to break the brick?



Solution 2.6-3 Standard brick in compression



A = 2.5 in.  $\times 4.0$  in. = 10.0 in.<sup>2</sup>

Maximum normal stress:

$$\sigma_x = \frac{P}{A}$$

Maximum shear stress:

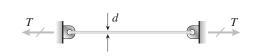
$$\tau_{\max} = \frac{\sigma_x}{2} = \frac{P}{2A}$$
  

$$\tau_{ult} = 3600 \text{ psi} \qquad \tau_{ult} = 1200 \text{ psi}$$
  
Because  $\tau_{ULT}$  is less than one-half of  $\sigma_{ULT}$ , the shear tress governs.

$$\tau_{\max} = \frac{P}{2A} \quad \text{or} \quad P_{\max} = 2A\tau_{ult}$$
$$P_{\max} = 2(10.0 \text{ in.}^2)(1200 \text{ psi})$$
$$= 24,000 \text{ lb} \longleftarrow$$

**Problem 2.6-4** A brass wire of diameter d = 2.42 mm is stretched tightly between rigid supports so that the tensile force is T = 92 N (see figure).

What is the maximum permissible temperature drop  $\Delta T$  if the allowable shear stress in the wire is 60 MPa? (The coefficient of thermal expansion for the wire is  $20 \times 10^{-6/\circ}$ C and the modulus of elasticity is 100 GPa.)



Probs. 2.6-4 and 2.6-5

.....

Solution 2.6-4 Brass wire in tension d = 2.42 mm $A = \frac{\pi d^2}{4} = 4.60 \text{ mm}^2$  $\alpha = 20 \times 10^{-6} \text{/}^{\circ}\text{C} \quad E = 100 \text{ GPa} \quad \tau_{\text{allow}} = 60 \text{ MPa}$ Initial tensile force: T = 92 N Stress due to initial tension:  $\sigma_x = \frac{T}{A}$ Stress due to temperature drop:  $\sigma_r = E\alpha(\Delta T)$ (see Eq. 2-18 of Section 2.5) Total stress:  $\sigma_x = \frac{T}{\Delta} + E\alpha(\Delta T)$ 

MAXIMUM SHEAR STRESS

$$\tau_{\max} = \frac{\sigma_x}{2} = \frac{1}{2} \left[ \frac{T}{A} + E\alpha(\Delta T) \right]$$

Solve for temperature drop  $\Delta T$ :

$$\Delta T = \frac{2\tau_{\max} - T/A}{E\alpha} \qquad \tau_{\max} = \tau_{\text{allow}}$$

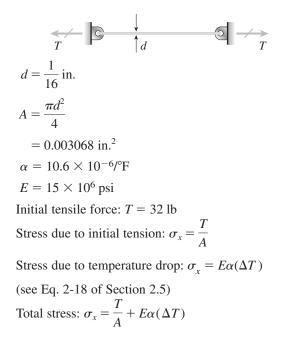
SUBSTITUTE NUMERICAL VALUES:

$$\Delta T = \frac{2(60 \text{ MPa}) - (92 \text{ N})/(4.60 \text{ mm}^2)}{(100 \text{ GPa})(20 \times 10^{-6})^{\circ}\text{C})}$$
$$= \frac{120 \text{ MPa} - 20 \text{ MPa}}{2 \text{ MPa}/^{\circ}\text{C}} = 50^{\circ}\text{C} \longleftarrow$$

**Problem 2.6-5** A brass wire of diameter d = 1/16 in. is stretched between rigid supports with an initial tension *T* of 32 lb (see figure).

- (a) If the temperature is lowered by 50°F, what is the maximum shear stress  $\tau_{\rm max}$  in the wire?
- (b) If the allowable shear stress is 10,000 psi, what is the maximum permissible temperature drop? (Assume that the coefficient of thermal expansion is  $10.6 \times 10^{-6}$ /°F and the modulus of elasticity is  $15 \times 10^{6}$  psi.)

Solution 2.6-5 Brass wire in tension



(a) Maximum shear stress when temperature drops  $50^{\circ}F$ 

$$\tau_{\max} = \frac{\sigma_x}{2} = \frac{1}{2} \left[ \frac{T}{A} + E\alpha(\Delta T) \right]$$
(Eq. 1)

Substitute numerical values:

$$\tau_{\rm max} = 9,190 \ {\rm psi} \longleftarrow$$

(b) MAXIMUM PERMISSIBLE TEMPERATURE DROP IF  $\tau_{\rm allow} = 10,000~{\rm psi}$ 

Solve Eq. (1) for 
$$\Delta T$$
:

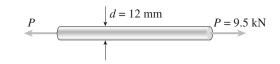
$$\Delta T = \frac{2\tau_{\rm max} - T/A}{E\alpha} \quad \tau_{\rm max} = \tau_{\rm allow}$$

Substitute numerical values:

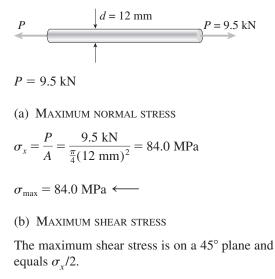
$$\Delta T = 60.2^{\circ} \text{F} \longleftarrow$$

**Problem 2.6-6** A steel bar with diameter d = 12 mm is subjected to a tensile load P = 9.5 kN (see figure).

- (a) What is the maximum normal stress  $\sigma_{\rm max}$  in the bar?
- (b) What is the maximum shear stress  $\tau_{\rm max}$ ?
- (c) Draw a stress element oriented at 45° to the axis of the bar and show all stresses acting on the faces of this element.



#### Solution 2.6-6 Steel bar in tension

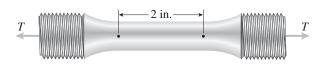


$$\tau_{\max} = \frac{\sigma_x}{2} = 42.0 \text{ MPa} \longleftarrow$$

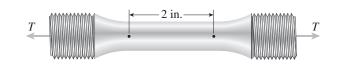
NOTE: All stresses have units of MPa.

**Problem 2.6-7** During a tension test of a mild-steel specimen (see figure), the extensioneter shows an elongation of 0.00120 in. with a gage length of 2 in. Assume that the steel is stressed below the proportional limit and that the modulus of elasticity  $E = 30 \times 10^6$  psi.

- (a) What is the maximum normal stress  $\sigma_{\rm max}$  in the specimen?
- (b) What is the maximum shear stress  $\tau_{\rm max}$ ?
- (c) Draw a stress element oriented at an angle of 45° to the axis of the bar and show all stresses acting on the faces of this element.



Solution 2.6-7 Tension test



Elongation:  $\delta = 0.00120$  in.

(2 in. gage length)

Strain:  $\varepsilon = \frac{\delta}{L} = \frac{0.00120 \text{ in.}}{2 \text{ in.}} = 0.00060$ 

Hooke's law :  $\sigma_x = E\varepsilon = (30 \times 10^6 \text{ psi})(0.00060)$ 

= 18,000 psi

(a) MAXIMUM NORMAL STRESS

 $\sigma_{\rm r}$  is the maximum normal stress.

 $\sigma_{\rm max}$  = 18,000 psi  $\leftarrow$ 

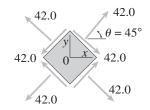
(b) MAXIMUM SHEAR STRESS

The maximum shear stress is on a 45° plane and equals  $\sigma_{\rm x}/2$ .

$$\tau_{\max} = \frac{\sigma_x}{2} = 9,000 \text{ psi} \longleftarrow$$

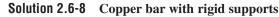
(c) Stress element at  $\theta = 45^{\circ}$ 

Note: All stresses have units of psi.

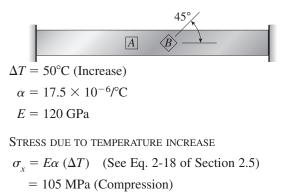


**Problem 2.6-8** A copper bar with a rectangular cross section is held without stress between rigid supports (see figure). Subsequently, the temperature of the bar is raised 50°C.

Determine the stresses on all faces of the elements *A* and *B*, and show these stresses on sketches of the elements. (Assume  $\alpha = 17.5 \times 10^{-6}$ /°C and E = 120 GPa.)



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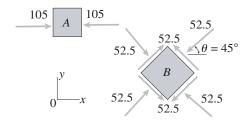
MAXIMUM SHEAR STRESS

$$\tau_{\max} = \frac{\sigma_x}{2}$$

= 52.5 MPa



STRESSES ON ELEMENTS A and B

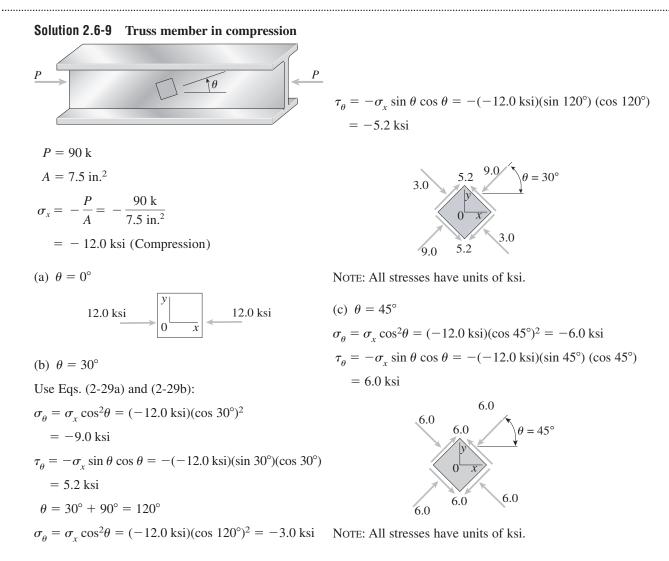


NOTE: All stresses have units of MPa.

**Problem 2.6-9** A compression member in a bridge truss is fabricated from a wide-flange steel section (see figure). The cross-sectional area A = 7.5 in.<sup>2</sup> and the axial load P = 90 k.

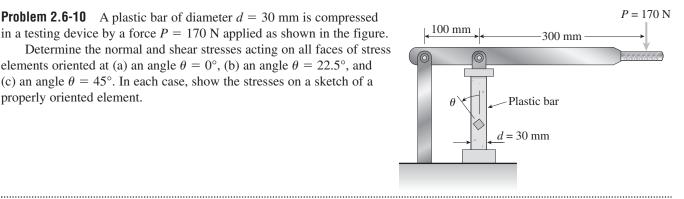
Determine the normal and shear stresses acting on all faces of stress elements located in the web of the beam and oriented at (a) an angle  $\theta = 0^{\circ}$ , (b) an angle  $\theta = 30^{\circ}$ , and (c) an angle  $\theta = 45^{\circ}$ . In each case, show the stresses on a sketch of a properly oriented element.

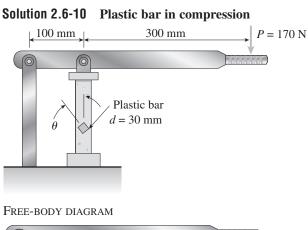




**Problem 2.6-10** A plastic bar of diameter d = 30 mm is compressed in a testing device by a force P = 170 N applied as shown in the figure.

Determine the normal and shear stresses acting on all faces of stress elements oriented at (a) an angle  $\theta = 0^{\circ}$ , (b) an angle  $\theta = 22.5^{\circ}$ , and (c) an angle  $\theta = 45^{\circ}$ . In each case, show the stresses on a sketch of a properly oriented element.







$$F =$$
Compressive force in plastic bar

$$F = 4P = 4(1/0 \text{ N}) = 680 \text{ N}$$

PLASTIC BAR (ROTATED TO THE HORIZONTAL)

$$\sigma_x = -\frac{F}{A} = -\frac{680 \text{ N}}{\frac{\pi}{4}(30 \text{ mm})^2}$$

$$= -962.0 \text{ kPa (Compression)}$$
(a)  $\theta = 0^\circ$ 

$$962 \text{ kPa} \qquad 962 \text{ kPa}$$

(b)  $\theta = 22.5^{\circ}$ 

Use Eqs. (2-29a) and (2-29b)

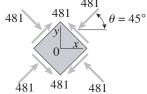
$$\sigma_{\theta} = \sigma_x \cos^2 \theta = (-962.0 \text{ kPa})(\cos 22.5^\circ)^2$$
$$= -821 \text{ kPa}$$

$$\tau_{\theta} = -\sigma_{x} \sin \theta \cos \theta$$
  
= -(-962.0 kPa)(sin 22.5°)(cos 22.5°)  
= 340 kPa  
$$\theta = 22.5^{\circ} + 90^{\circ} = 112.5^{\circ}$$
$$\sigma_{\theta} = \sigma_{x} \cos^{2}\theta = (-962.0 \text{ kPa})(\cos 112.5^{\circ})^{2}$$
  
= -141 kPa  
$$\tau_{\theta} = -\sigma_{x} \sin \theta \cos \theta$$
  
= -(-962.0 kPa)(sin 112.5°)(cos 112.5°)  
= -340 kPa  
$$141 \qquad 340 \qquad 821 \qquad \theta = 22.5^{\circ}$$
$$821 \qquad 340 \qquad 141 \qquad 821 \qquad \theta = 22.5^{\circ}$$

NOTE: All stresses have units of kPa.

(c) 
$$\theta = 45^{\circ}$$
  
 $\sigma_{\theta} = \sigma_x \cos^2 \theta = (-962.0 \text{ kPa})(\cos 45^{\circ})^2$   
 $= -481 \text{ kPa}$   
 $\tau_{\theta} = -\sigma_x \sin \theta \cos \theta$   
 $= -(-962.0 \text{ kPa})(\sin 45^{\circ})(\cos 45^{\circ}) = 481 \text{ kPa}$   
481

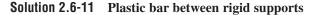
141



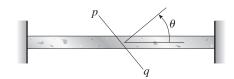
NOTE: All stresses have units of kPa.

**Problem 2.6-11** A plastic bar fits snugly between rigid supports at room temperature ( $68^{\circ}$ F) but with no initial stress (see figure). When the temperature of the bar is raised to  $160^{\circ}$ F, the compressive stress on an inclined plane *pq* becomes 1700 psi.

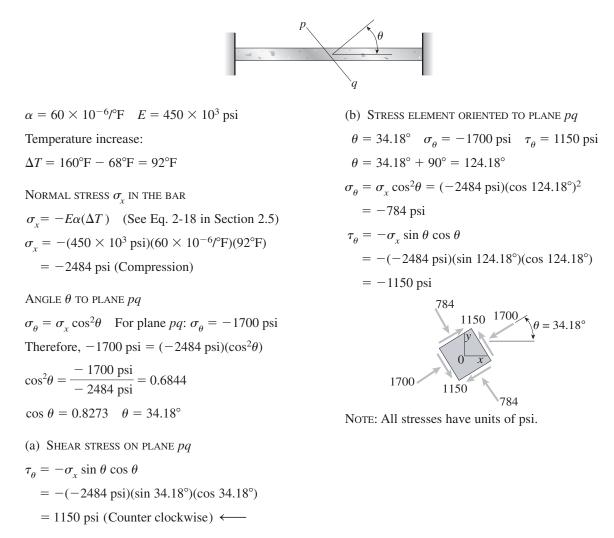
- (a) What is the shear stress on plane pq? (Assume  $\alpha = 60 \times 10^{-6}$ /°F and  $E = 450 \times 10^{3}$  psi.)
- (b) Draw a stress element oriented to plane *pq* and show the stresses acting on all faces of this element.



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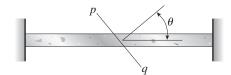
Probs. 2.6-11 and 2.6-12



**Problem 2.6-12** A copper bar is held snugly (but without any initial stress) between rigid supports (see figure). The allowable stresses on the inclined plane pq, for which  $\theta = 55^{\circ}$ , are specified as 60 MPa in compression and 30 MPa in shear.

- (a) What is the maximum permissible temperature rise  $\Delta T$  if the allowable stresses on plane pq are not to be exceeded? (Assume  $\alpha = 17 \times 10^{-6}$ /°C and E = 120 GPa.)
- (b) If the temperature increases by the maximum permissible amount, what are the stresses on plane *pq*?

#### Solution 2.6-12 Copper bar between rigid supports



 $\alpha = 17 \times 10^{-6} / ^{\circ} \mathrm{C}$ 

E = 120 GPa

Plane  $pq: \theta = 55^{\circ}$ 

Allowable stresses on plane pq:

 $\sigma_{\text{allow}} = 60 \text{ MPa} \text{ (Compression)}$ 

$$\tau_{\text{allow}} = 30 \text{ MPa} \text{ (Shear)}$$

(a) Maximum permissible temperature rise  $\Delta T$ 

$$\sigma_{\theta} = \sigma_x \cos^2 \theta \quad -60 \text{ MPa} = \sigma_x (\cos 55^\circ)^2$$
$$\sigma_x = -182.4 \text{ MPa}$$
$$\tau_{\theta} = -\sigma_x \sin \theta \cos \theta$$
$$30 \text{ MPa} = -\sigma_x (\sin 55^\circ)(\cos 55^\circ)$$
$$\sigma_x = -63.85 \text{ MPa}$$

Shear stress governs.  $\sigma_x = -63.85$  MPa Due to temperature increase  $\Delta T$ :  $\sigma_x = -E\alpha(\Delta T)$  (See Eq. 2-18 in Section 2.5) -63.85 MPa =  $-(120 \text{ GPa})(17 \times 10^{-6})^{\circ}\text{C})(\Delta T)$  $\Delta T = 31.3^{\circ}\text{C} \longleftarrow$ 

(b) Stresses on plane pq

$$\sigma_x = -63.85 \text{ MPa}$$

 $\sigma_{\theta} = \sigma_x \cos^2 \theta = (-63.85 \text{ MPa})(\cos 55^\circ)^2$ 

= -21.0 MPa (Compression)  $\leftarrow$ 

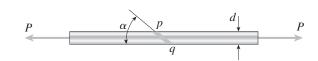
$$\tau_{\theta} = -\sigma_x \sin \theta \cos \theta$$

$$= -(-63.85 \text{ MPa})(\sin 55^{\circ})(\cos 55^{\circ})$$

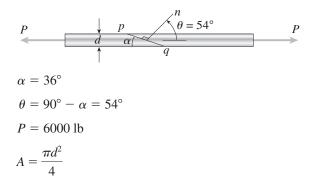
 $= 30.0 \text{ MPa} (\text{Counter clockwise}) \longleftarrow$ 

**Problem 2.6-13** A circular brass bar of diameter *d* is composed of two segments brazed together on a plane pq making an angle  $\alpha = 36^{\circ}$  with the axis of the bar (see figure). The allowable stresses in the brass are 13,500 psi in tension and 6500 psi in shear. On the brazed joint, the allowable stresses are 6000 psi in tension and 3000 psi in shear.

If the bar must resist a tensile force P = 6000 lb, what is the minimum required diameter  $d_{\min}$  of the bar?



## Solution 2.6-13 Brass bar in tension



Stress  $\sigma_{\rm x}$  based upon allowable stresses in the brass

Tensile stress ( $\theta = 0^{\circ}$ ):  $\sigma_{\text{allow}} = 13,500 \text{ psi}$ 

$$\sigma_x = 13,500 \text{ psi} \tag{1}$$

Shear stress ( $\theta = 45^{\circ}$ ):  $\tau_{\text{allow}} = 6500 \text{ psi}$ 

$$\tau_{\max} = \frac{\sigma_x}{2}$$

$$\sigma_x = 2 \tau_{\text{allow}}$$

$$= 13,000 \text{ psi}$$
(2)

Stress  $\sigma_x$  based upon allowable stresses on the brazed joint ( $\theta = 54^{\circ}$ )

 $\sigma_{\text{allow}} = 6000 \text{ psi (tension)}$  $\tau_{\text{allow}} = 3000 \text{ psi (shear)}$ 

Tensile stress: 
$$\sigma_{\theta} = \sigma_x \cos^2 \theta$$
  
 $\sigma_x = \frac{\sigma_{\text{allow}}}{\cos^2 \theta} = \frac{6000 \text{ psi}}{(\cos 54^\circ)^2}$   
= 17,370 psi (3)

Shear stress:  $\tau_{\theta} = -\sigma_x \sin \theta \cos \theta$ 

$$\sigma_{x} = \left| \frac{\tau_{\text{allow}}}{\sin \theta \cos \theta} \right| = \frac{3,000 \text{ psi}}{(\sin 54^{\circ})(\cos 54^{\circ})}$$
$$= 6,310 \text{ psi}$$
(4)

ALLOWABLE STRESS

Compare (1), (2), (3), and (4).

Shear stress on the brazed joint governs.

 $\sigma_x = 6310 \text{ psi}$ 

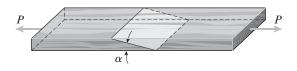
DIAMETER OF BAR

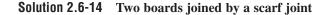
$$A = \frac{P}{\sigma_x} = \frac{6000 \text{ lb}}{6310 \text{ psi}} = 0.951 \text{ in.}^2$$
$$A = \frac{\pi d^2}{4} \quad d^2 = \frac{4A}{\pi} \quad d_{\min} = \sqrt{\frac{4A}{\pi}}$$

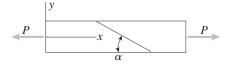
$$= 1.10$$
 in.  $\leftarrow$ 

**Problem 2.6-14** Two boards are joined by gluing along a scarf joint, as shown in the figure. For purposes of cutting and gluing, the angle  $\alpha$  between the plane of the joint and the faces of the boards must be between 10° and 40°. Under a tensile load *P*, the normal stress in the boards is 4.9 MPa.

- (a) What are the normal and shear stresses acting on the glued joint if  $\alpha = 20^{\circ}$ ?
- (b) If the allowable shear stress on the joint is 2.25 MPa, what is the largest permissible value of the angle  $\alpha$ ?
- (c) For what angle  $\alpha$  will the shear stress on the glued joint be numerically equal to twice the normal stress on the joint?



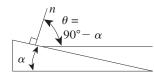




 $10^\circ \le \alpha \le 40^\circ$ 

Due to load *P*:  $\sigma_x = 4.9$  MPa

(a) Stresses on joint when  $\alpha = 20^{\circ}$ 



$$\theta = 90^{\circ} - \alpha = 70^{\circ}$$
  

$$\sigma_{\theta} = \sigma_x \cos^2 \theta = (4.9 \text{ MPa})(\cos 70^{\circ})^2$$
  

$$= 0.57 \text{ MPa} \longleftarrow$$
  

$$\tau_{\theta} = -\sigma_x \sin \theta \cos \theta$$
  

$$= (-4.9 \text{ MPa})(\sin 70^{\circ})(\cos 70^{\circ})$$

(b) Largest angle 
$$\alpha$$
 if  $\tau_{\text{allow}} = 2.25$  MPa

$$\tau_{\rm allow} = -\sigma_x \sin \theta \cos \theta$$

The shear stress on the joint has a negative sign. Its numerical value cannot exceed  $\tau_{\rm allow} = 2.25$  MPa. Therefore,

 $-2.25 \text{ MPa} = -(4.9 \text{ MPa})(\sin \theta)(\cos \theta) \text{ or}$  $\sin \theta \cos \theta = 0.4592$ 

From trigonometry:  $\sin \theta \cos \theta = \frac{1}{2} \sin 2\theta$ 

Therefore:  $\sin 2\theta = 2(0.4592) = 0.9184$ 

Solving :  $2\theta = 66.69^{\circ}$  or  $113.31^{\circ}$ 

 $\theta = 33.34^{\circ}$  or  $56.66^{\circ}$  $\alpha = 90^\circ - \theta$   $\therefore \alpha = 56.66^\circ$  or  $33.34^\circ$ Since  $\alpha$  must be between 10° and 40°, we select  $\alpha = 33.3^{\circ} \longleftarrow$ Note: If  $\alpha$  is between 10° and 33.3°,  $|\tau_{\theta}| < 2.25$  MPa. If  $\alpha$  is between 33.3° and 40°,  $|\tau_{\theta}| > 2.25$  MPa. (c) what is  $\alpha$  if  $\tau_{\theta} = 2\sigma_{\theta}$ ? Numerical values only:  $|\tau_{\theta}| = \sigma_x \sin \theta \cos \theta \qquad |\sigma_{\theta}| = \sigma_x \cos^2 \theta$  $\left|\frac{\tau_{\theta}}{\sigma_{\theta}}\right| = 2$  $\sigma_x \sin \theta \cos \theta = 2\sigma_x \cos^2 \theta$  $\sin \theta = 2 \cos \theta$  or  $\tan \theta = 2$  $\theta = 63.43^{\circ}$   $\alpha = 90^{\circ} - \theta$  $= 26.6^{\circ} \longleftarrow$ 

NOTE: For  $\alpha = 26.6^{\circ}$  and  $\theta = 63.4^{\circ}$ , we find  $\sigma_{\theta} = 0.98$  MPa and  $\tau_{\theta} = -1.96$  MPa.

Thus, 
$$\left|\frac{\tau_{\theta}}{\sigma_{\theta}}\right| = 2$$
 as required.

 $\tau_{\theta} \tau_{\theta}$ 

 $au_{ heta} \ au_{ heta}$ 

 $\sigma_{\theta} = 10,000 \text{ psi}$ 

 $\theta$ 

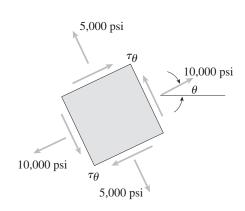
5,000 psi

**Problem 2.6-15** Acting on the sides of a stress element cut from a bar in uniaxial stress are tensile stresses of 10,000 psi and 5,000 psi, as shown in the figure.

- (a) Determine the angle  $\theta$  and the shear stress  $\tau_{\theta}$  and show all stresses on a sketch of the element.
- (b) Determine the maximum normal stress  $\sigma_{\rm max}$  and the maximum shear stress  $\tau_{\rm max}$  in the material.



.....



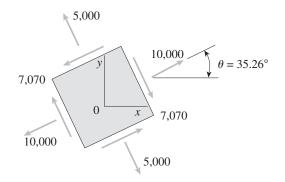
From Eq. (1) or (2):

 $\sigma_x = 15,000 \text{ psi}$   $\tan \theta = -\sigma_x \sin \theta \cos \theta$   $= (-15,000 \text{ psi})(\sin 35.26^\circ)(\cos 35.26^\circ)$  $= -7,070 \text{ psi} \longleftarrow$ 

5,000 psi

10,000 psi

Minus sign means that  $\tau_{\theta}$  acts clockwise on the plane for which  $\theta = 35.26^{\circ}$ .



NOTE: All stresses have units of psi.

(b) MAXIMUM NORMAL AND SHEAR STRESS

$$\sigma_{\max} = \sigma_x = 15,000 \text{ psi} \longleftarrow$$
  
 $\tau_{\max} = \frac{\sigma_x}{2} = 7,500 \text{ psi} \longleftarrow$ 

(a) Angle  $\theta$  and shear stress  $\tau_{\theta}$ 

$$\sigma_{\theta} = \sigma_{x} \cos^{2}\theta$$

$$\sigma_{\theta} = 10,000 \text{ psi}$$

$$\sigma_{x} = \frac{\sigma_{\theta}}{\cos^{2}\theta} = \frac{10,000 \text{ psi}}{\cos^{2}\theta}$$
(1)

Plane at angle  $\theta$  + 90°

$$\sigma_{\theta+90^{\circ}} = \sigma_x [\cos(\theta + 90^{\circ})]^2 = \sigma_x [-\sin\theta]^2$$
$$= \sigma_x \sin^2\theta$$
$$\sigma_{\theta+90^{\circ}} = 5,000 \text{ psi}$$
$$\sigma_x = \frac{\sigma_{\theta+90^{\circ}}}{\sin^2\theta} = \frac{5,000 \text{ psi}}{\sin^2\theta}$$
(2)

Equate (1) and (2):

$$\frac{10,000 \text{ psi}}{\cos^2 \theta} = \frac{5,000 \text{ psi}}{\sin^2 \theta}$$
$$\tan^2 \theta = \frac{1}{2} \quad \tan \theta = \frac{1}{\sqrt{2}} \quad \theta = 35.26^\circ \longleftarrow$$